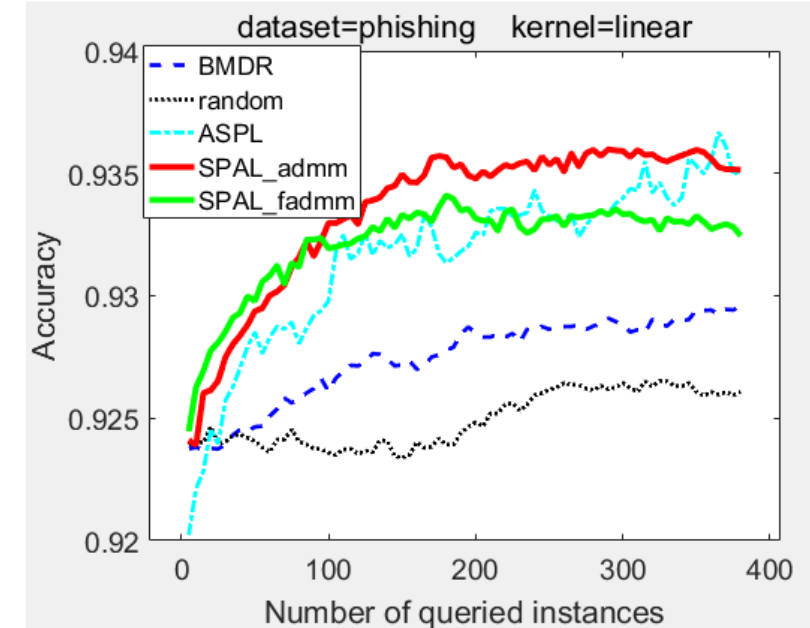
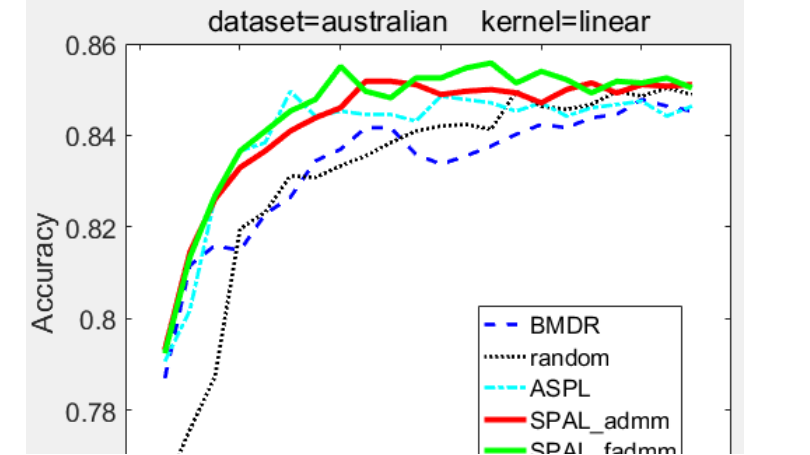
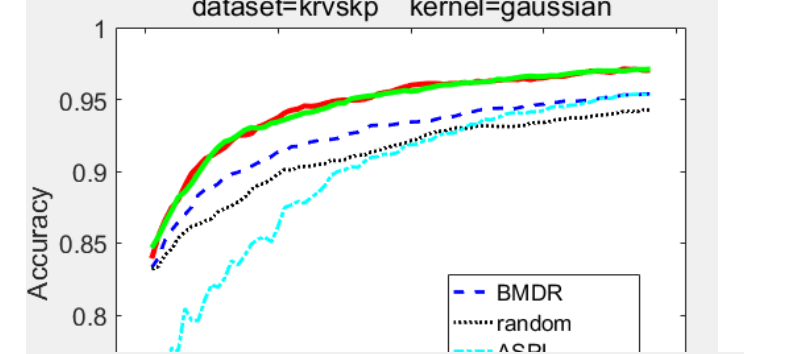
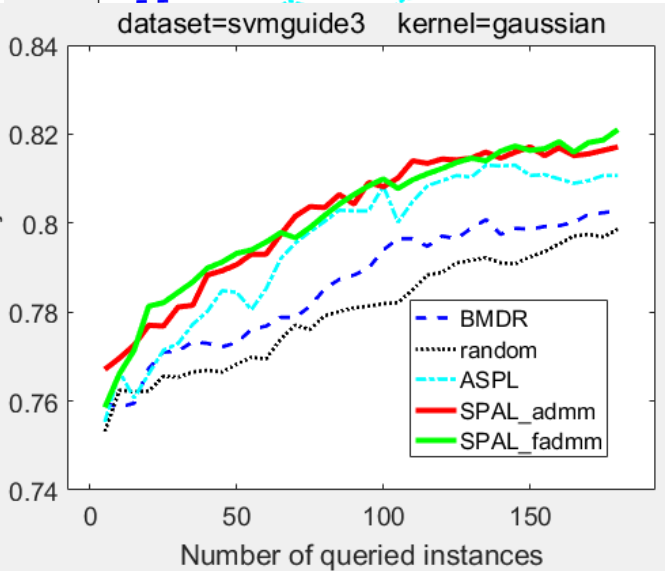
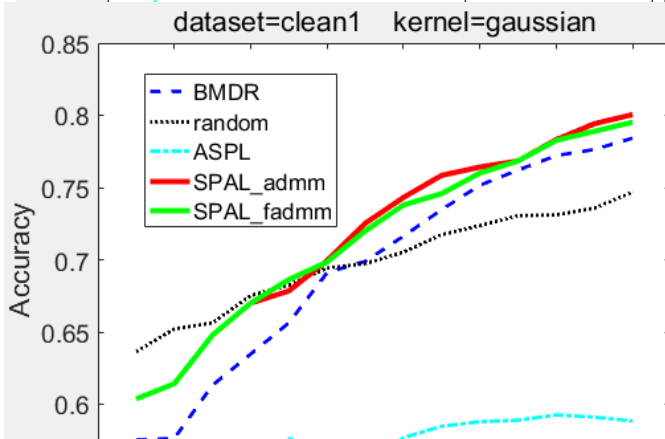
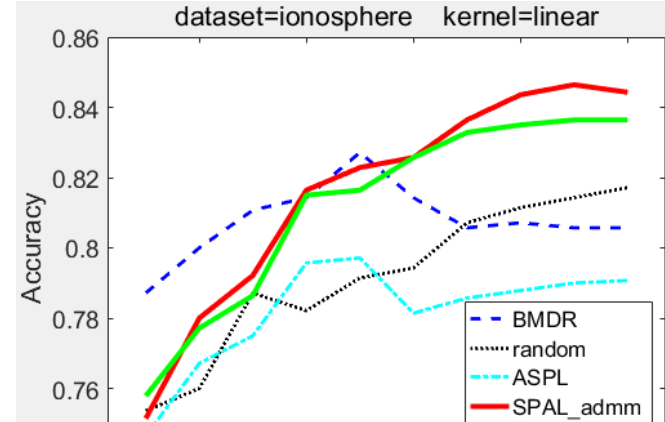
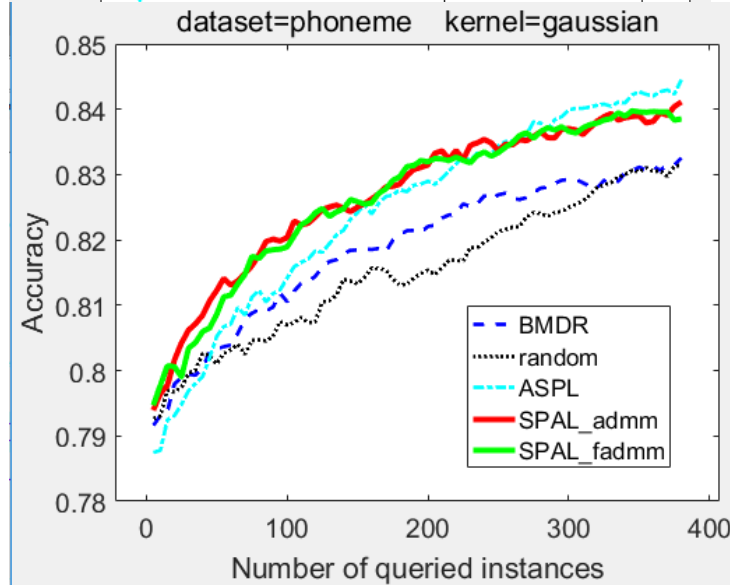
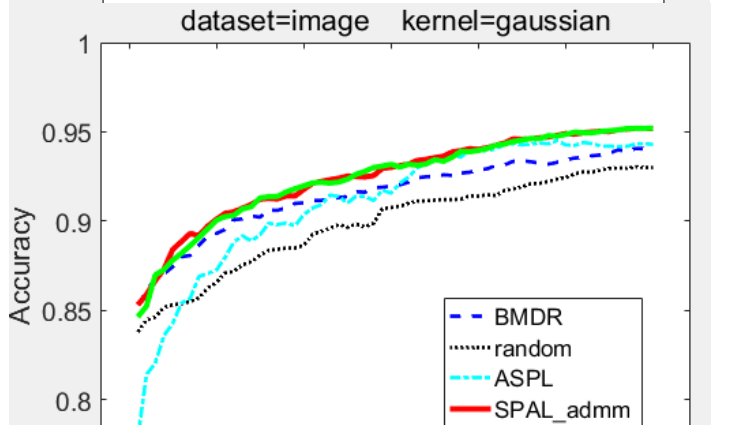
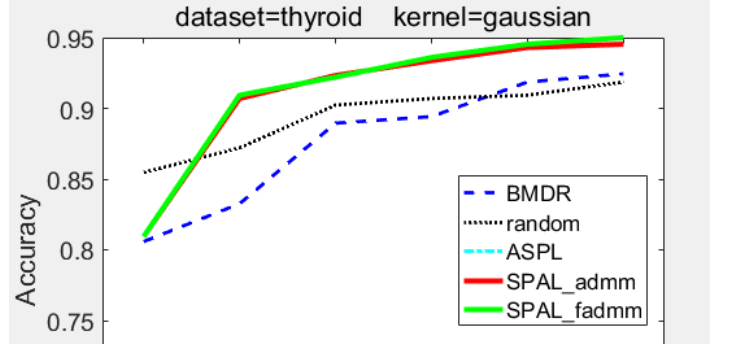


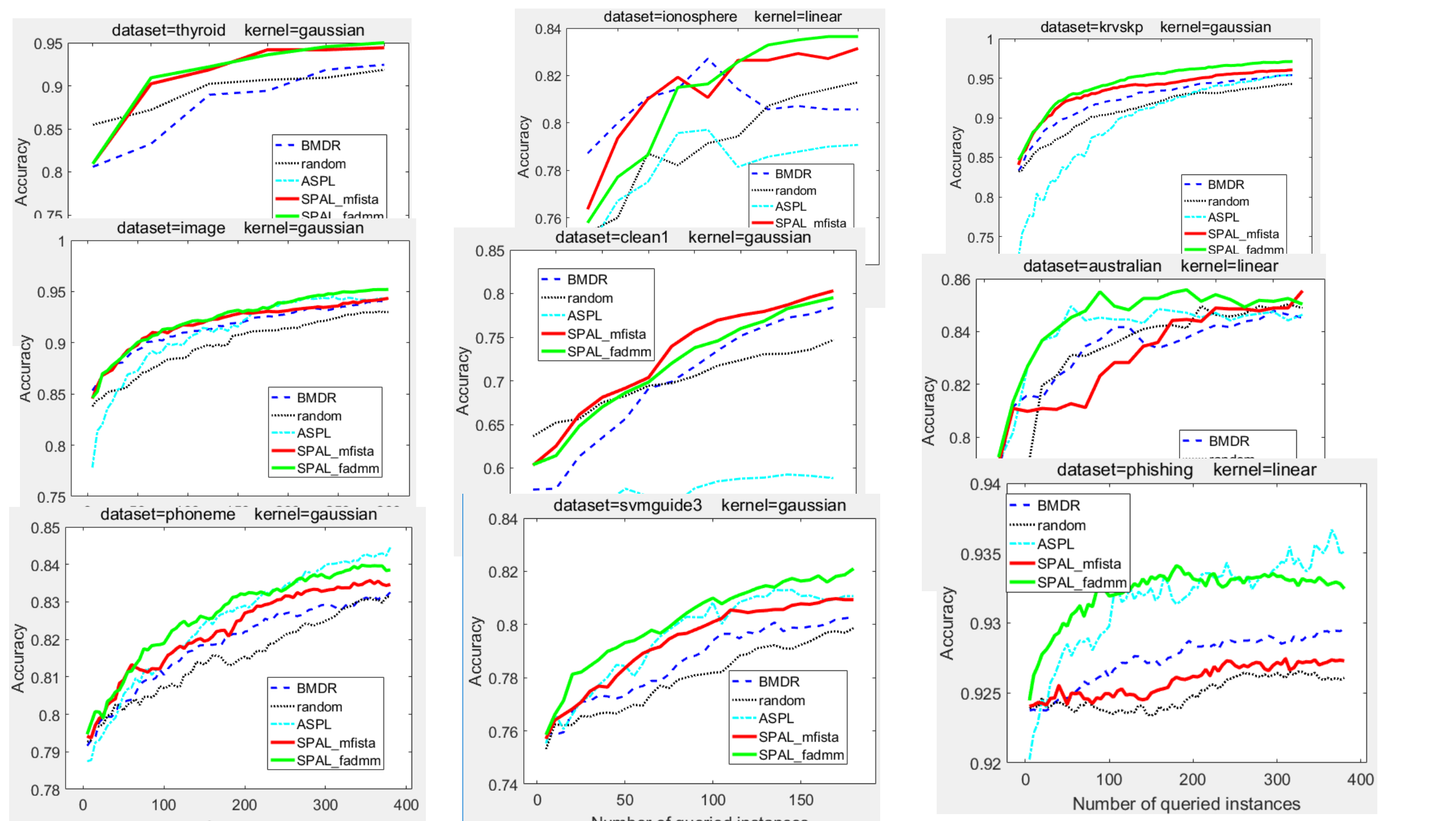
- 优化f时的判断**收敛精度**对性能影响很大，较小的精度一般性能会下降很多，也有极少数据集会变好
- 优化方法对性能影响较大
- 对label set的权去掉的话，性能在有些数据集变好有些数据集变差，有些变化不大
- 将SPL的权去掉的话，性能在大部分数据集上有所下降，小部分小的数据集有些上升
- 对参数 λ 的步长不太敏感，考虑测试一下初始值

- ADMM : 对约束条件放松 (红色)
- FADMM : 不放松约束, 但过滤掉权较小的样本 (绿色)

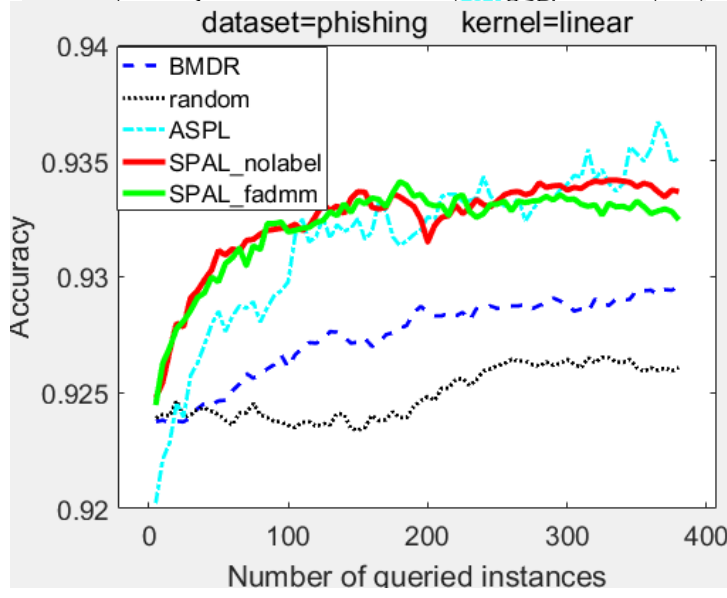
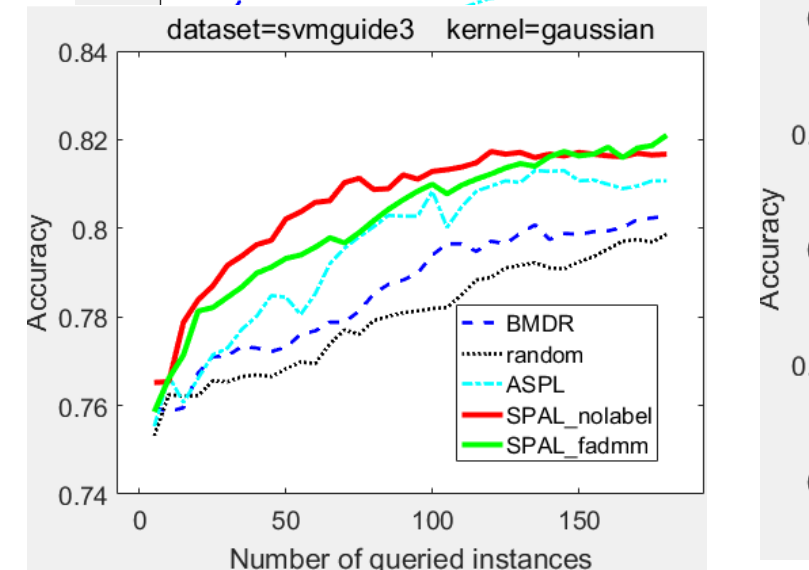
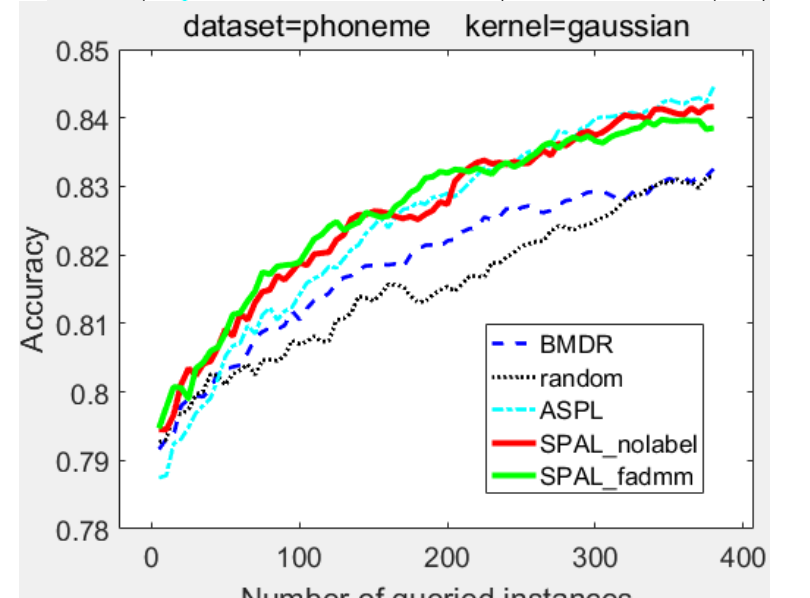
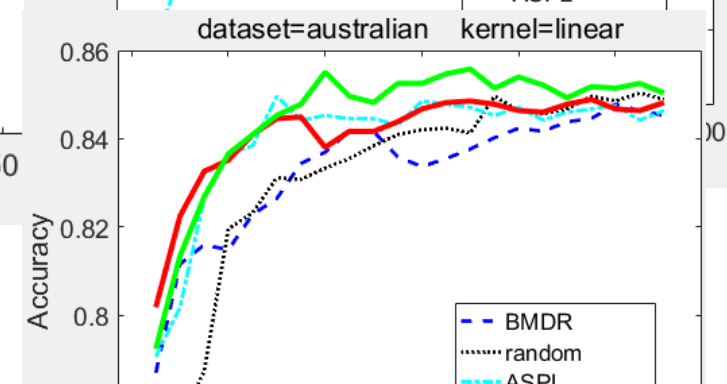
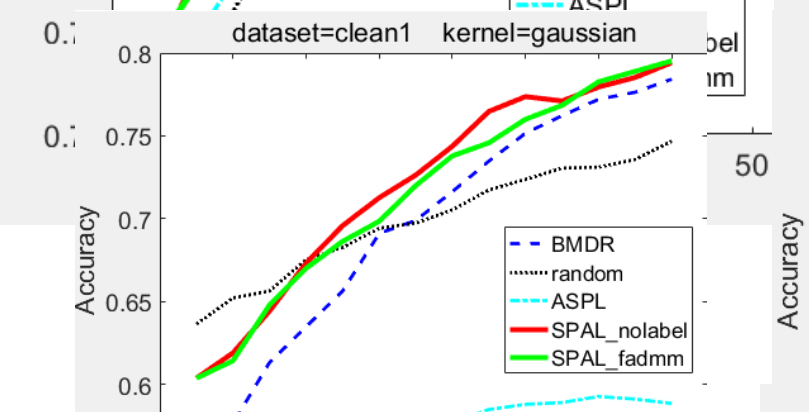
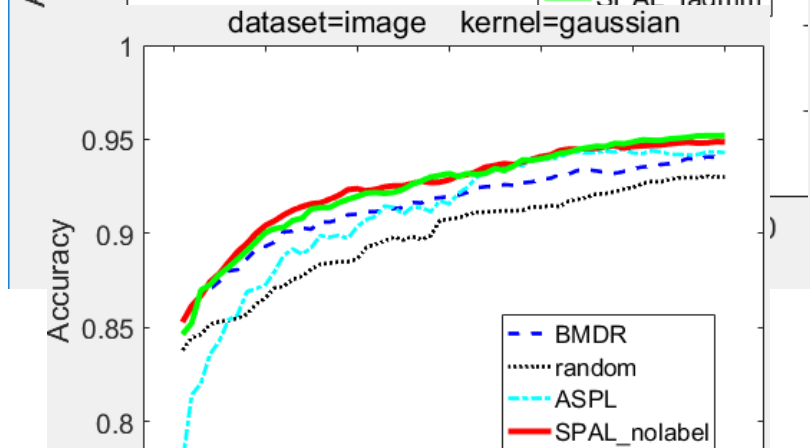
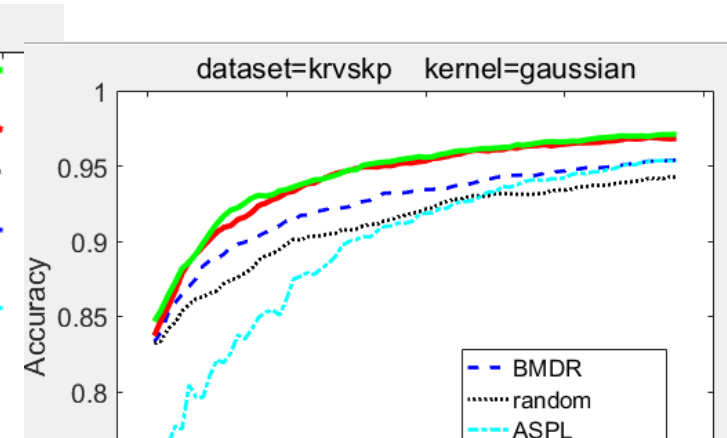
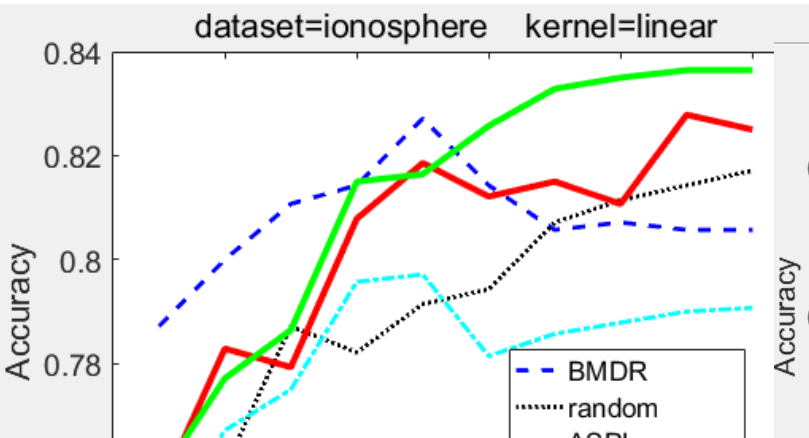
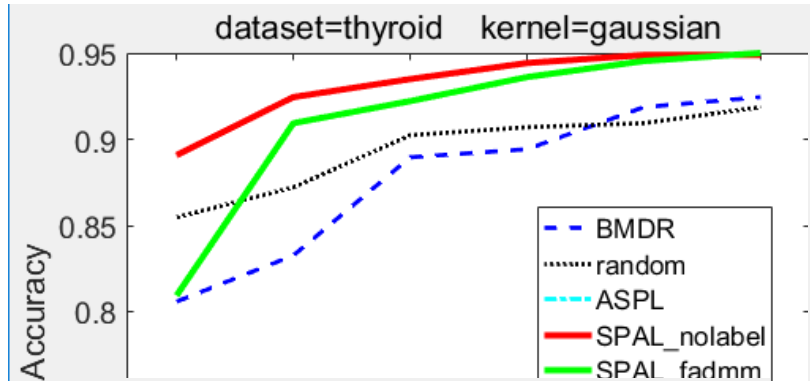
精度 : $1e-4$



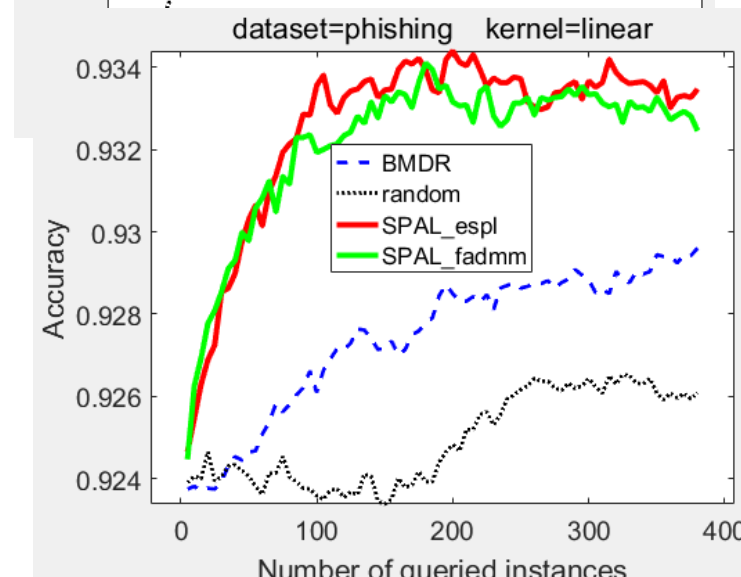
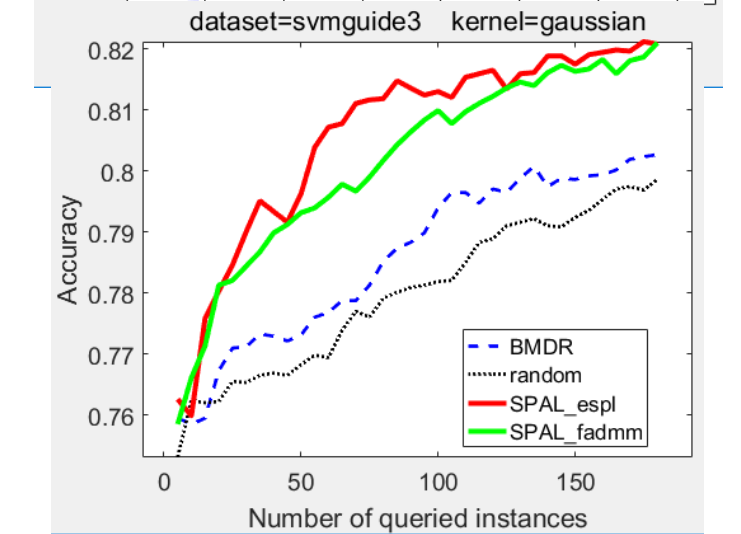
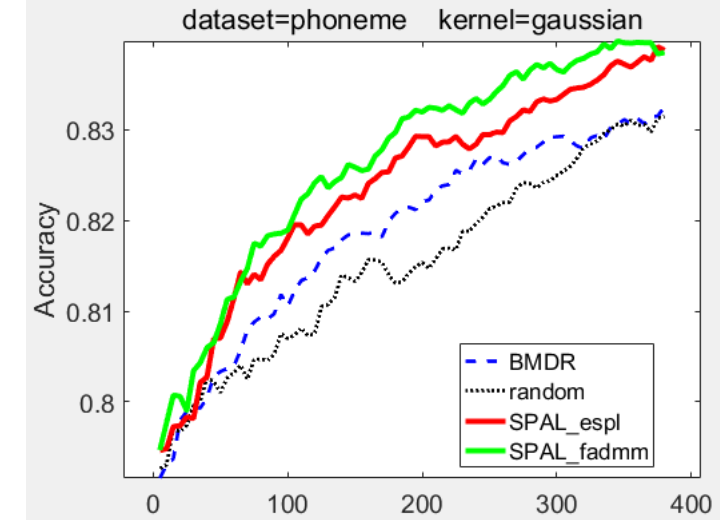
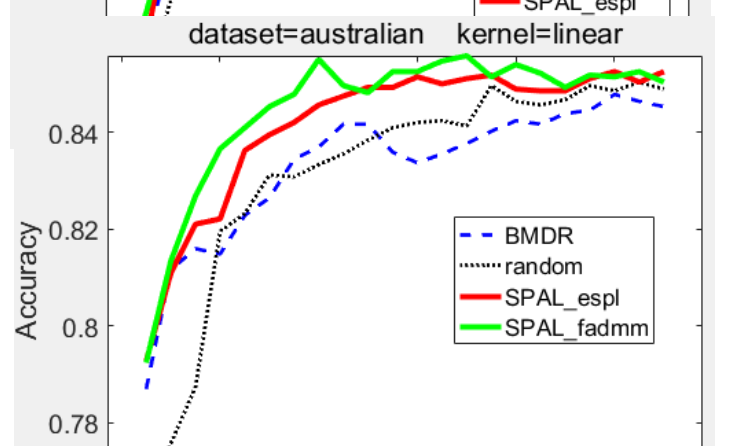
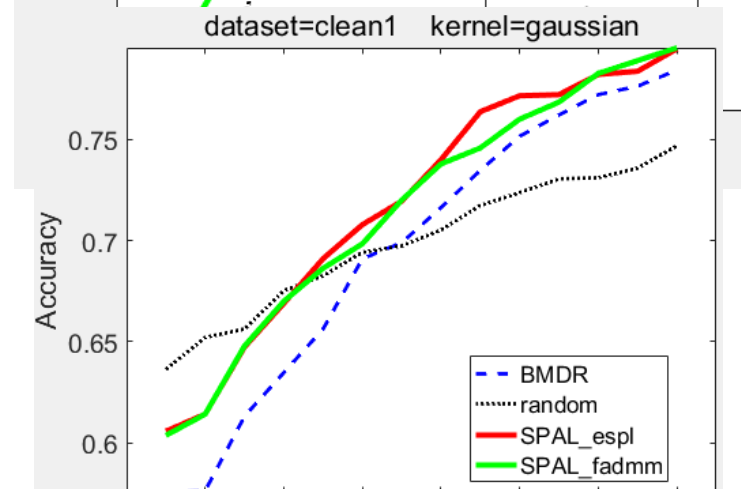
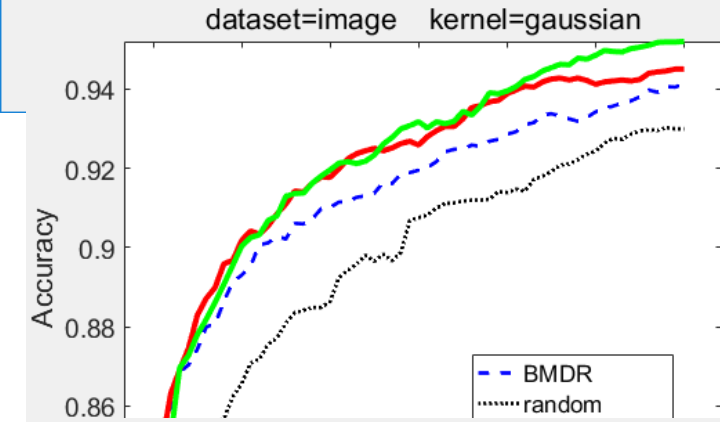
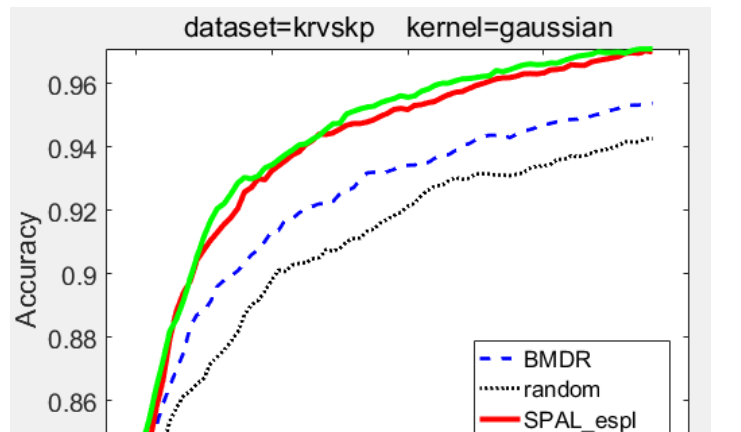
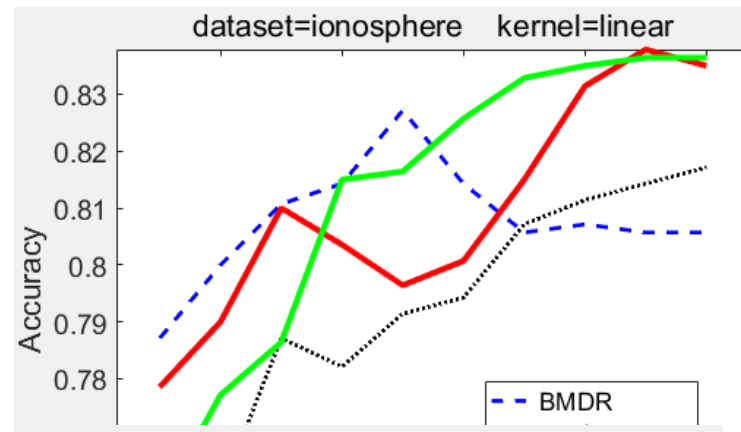
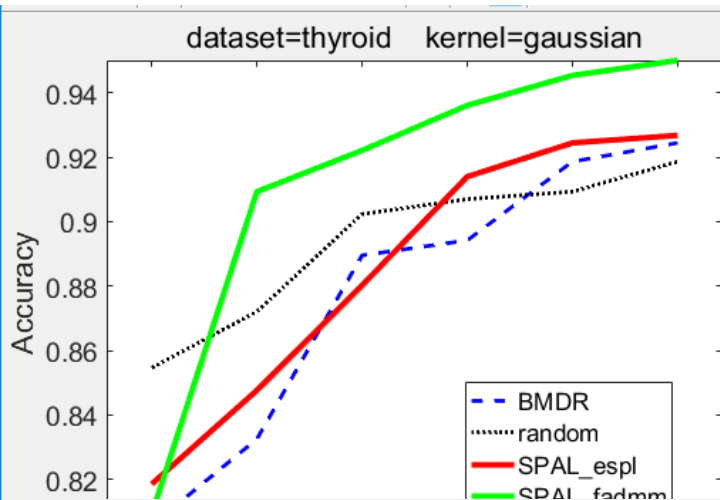
- MFISTA : 快速的近端梯度下降法
- FADMM : 不放松约束, 但过滤掉权较小的样本 (绿色)



- NOLABEL:去掉label set的权 (红色)
- FADMM : 不放松约束, 但过滤掉权较小的样本 (绿色)



- NOSPL :去掉 v (红色)
- FADMM :不放松约束, 但过滤掉权较小的样本 (绿色)



• QP :

$$v_j \cdot w_j \left(\hat{y}_j - f(\mathbf{x}_j) \right)^2 \quad \text{where } \hat{y}_j = -\text{sign}(f(\mathbf{x}_j))$$

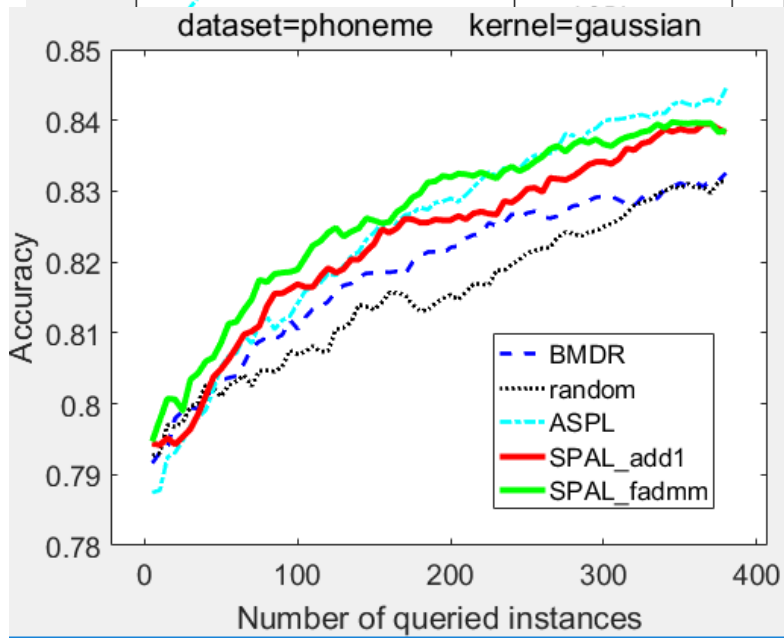
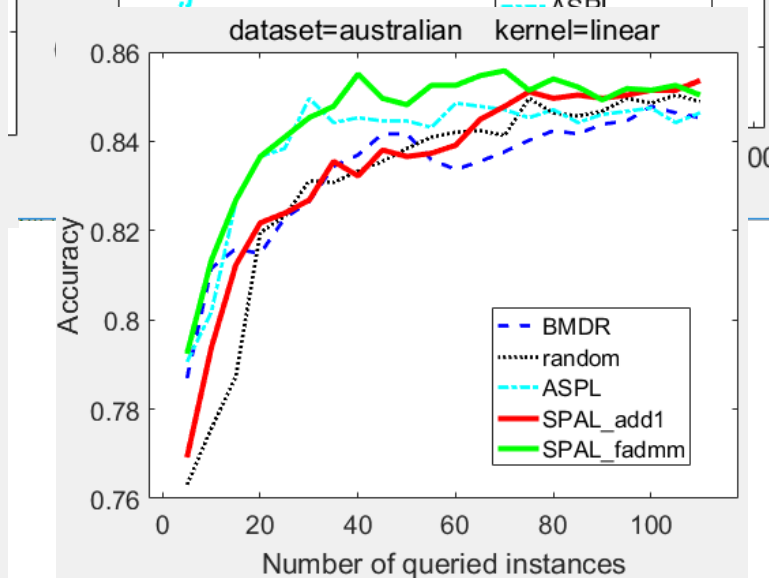
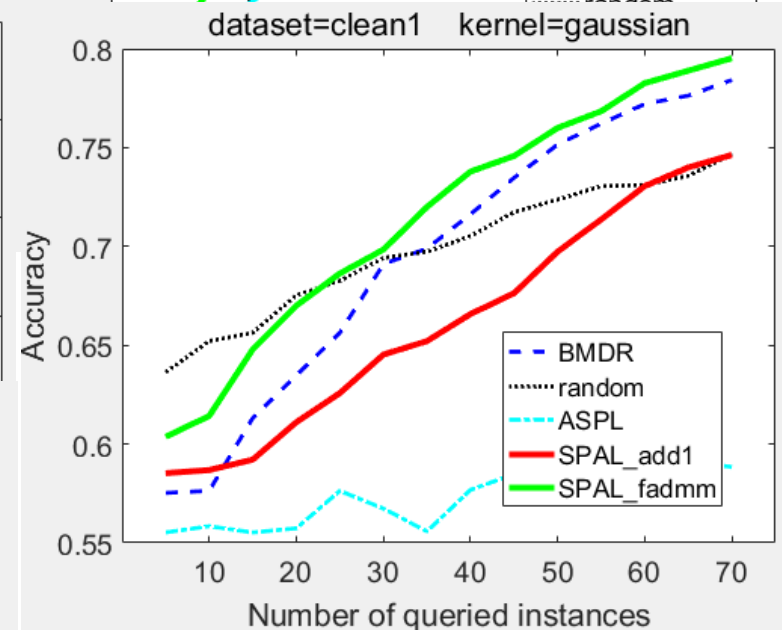
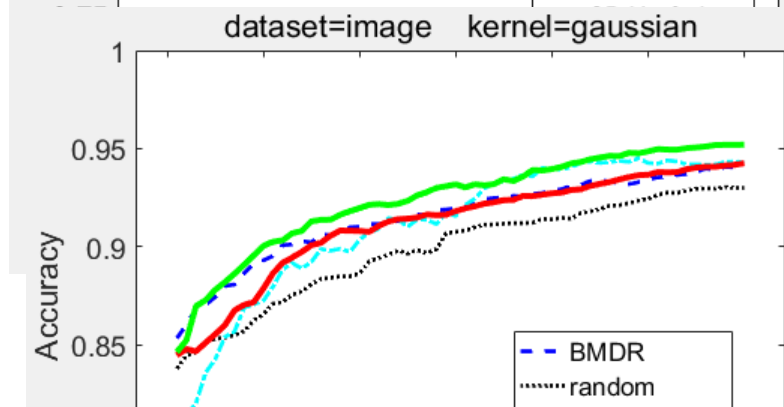
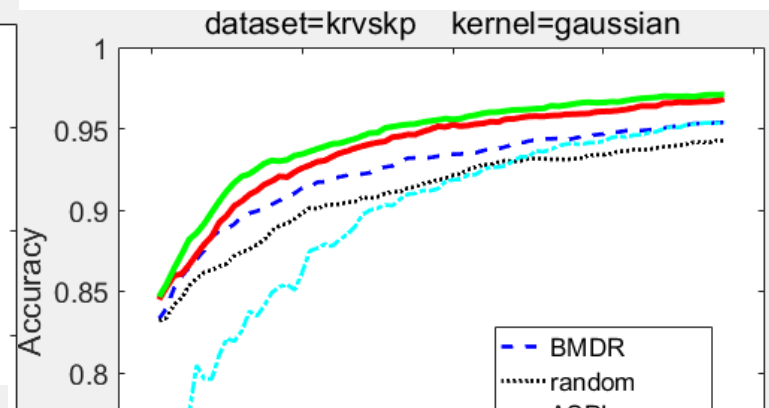
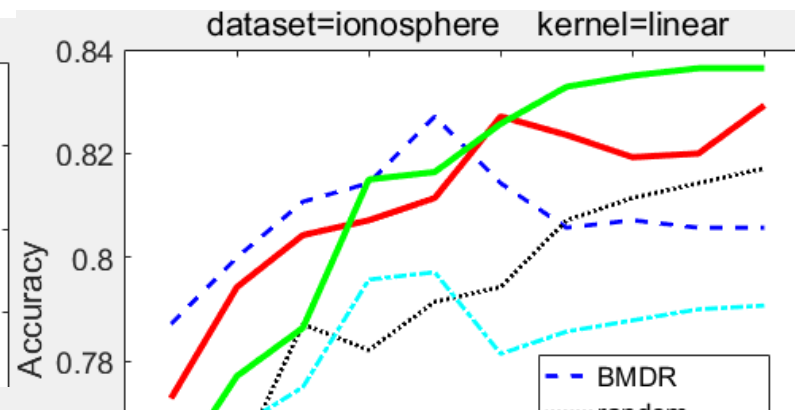
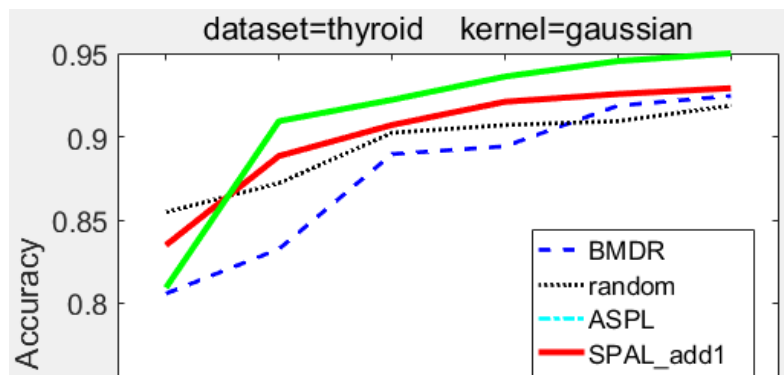
$$\text{We should have: } v_j \cdot w_j \left(f(\mathbf{x}_j)^2 + 2|f(\mathbf{x}_j)| + 1 \right)$$

which can be rewritten as

$$\min_{\alpha^T \mathbf{1}_u = b} \beta \alpha^T K_1 \alpha + (\beta \mathbf{k} + \mathbf{a}) \alpha,$$

where $a_j = \|\mathbf{w}^T \phi(\mathbf{x}_j)\|_2^2 + 2|\mathbf{w}^T \phi(\mathbf{x}_j)|$. This

- ADD1 :QP和更新SPL权的时候+1
- FADMM :不放松约束, 但过滤掉权较小的样本 (绿色)



原目标:

$$\min_{f,w,v} \sum_{i=1}^{n_l} \left[v_i (y_i - f(x_i))^2 + \lambda \left(\frac{1}{2} v_i^2 - v_i \right) \right] + \sum_{j=1}^{n_u} \left[v_j \cdot w_j \left(\hat{y}_j - f(x_j) \right)^2 + \lambda \left(\frac{1}{2} v_j^2 - v_j \right) \right] + \mu (w^T K_1 w + kw) + \gamma \|f\|^2$$

$w_j \in [0,1], v_i \in [0,1] \quad \forall i=1 \dots n$

参数w对应信息量和代表性, 参数v对应样本的难易程度

新目标:

$$\min_{f,w} \sum_{i=1}^{n_l} [(y_i - f(x_i))^2] + \sum_{j=1}^{n_u} \left[w_j \left(\hat{y}_j - f(x_j) \right)^2 + w_j T(f, \lambda) \right] + \mu (w^T K_1 w + kw) + \gamma \|f\|^2$$

$w_j \in [0,1] \quad \forall i=1 \dots n$

仅有参数w, 一项对应信息量, 一项对应代表性, 一项 $T(f, \lambda)$ 对应样本的难易程度

思路: 样本损失 $(\hat{y}_j - f(x_j))^2$ 超过 λ 时, $T(f, \lambda)$ 会快速上升, 小于 λ 时, 值较小, 如sigmoid函数, 指数函数, $x e^x$, hinge_loss等等

取指数函数:

$$\min_{f,w} \sum_{i=1}^{n_l} [(y_i - f(x_i))^2] + \sum_{j=1}^{n_u} \left[w_j (\hat{y}_j - f(x_j))^2 + w_j \tau (\hat{y}_j - f(x_j))^2 - \lambda \right] + \mu(w^T K_1 w + kw) + \gamma \|f\|^2$$
$$w_j \in [0,1] \quad \forall i=1 \dots n$$

Where τ is a constant

优化f时:

$$\min_{\theta} \sum_{i=1}^{n_l} \left(y_i - \sum_{x_k \in L} \theta_k k(x_k, x_i) \right)^2 + \sum_{j=1}^{n_u} \left[w_j \left(\sum_{x_k \in L} \theta_k k(x_k, x_j) \right)^2 + 2w_j \left| \sum_{x_k \in L} \theta_k k(x_k, x_j) \right| \right]$$

取类似于Hinge_loss的分段函数:

$$\min_{f,w} \sum_{i=1}^{n_l} [(y_i - f(x_i))^2] + \sum_{j=1}^{n_u} \left[w_j (\hat{y}_j - f(x_j))^2 + w_j \max(0, (\hat{y}_j - f(x_j))^2 - \lambda) \right] + \mu(w^T K_1 w + kw) + \gamma \|f\|^2$$

s. t $w_j \in [0,1] \quad \forall i=1 \dots n$

$$\min_{f,w} \sum_{i=1}^{n_l} [(y_i - f(x_i))^2] + \sum_{j=1}^{n_u} \left[w_j (\hat{y}_j - f(x_j))^2 + w_j \xi_j \right] + \mu(w^T K_1 w + kw) + \gamma \|f\|^2$$

$w_j \in [0,1] \quad \forall i=1 \dots n$
 $(\hat{y}_j - f(x_j))^2 - \lambda + \xi_j \geq 0$

优化f时:

$$\min_{\theta, \xi} \sum_{i=1}^{n_l} \left(y_i - \sum_{x_k \in L} \theta_k k(x_k, x_i) \right)^2 + \sum_{j=1}^{n_u} \left[w_j \left(\sum_{x_k \in L} \theta_k k(x_k, x_j) \right)^2 + 2w_j \left| \sum_{x_k \in L} \theta_k k(x_k, x_j) \right| + w_j \xi_j \right] + \gamma \theta^T K_{LL} \theta$$

$f(x_j)^2 + 2|f(x_j)| + 1 - \lambda + \xi_j \geq 0$