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# Noise-resistant Deep Metric Learning with Ranking-based Instance Selection

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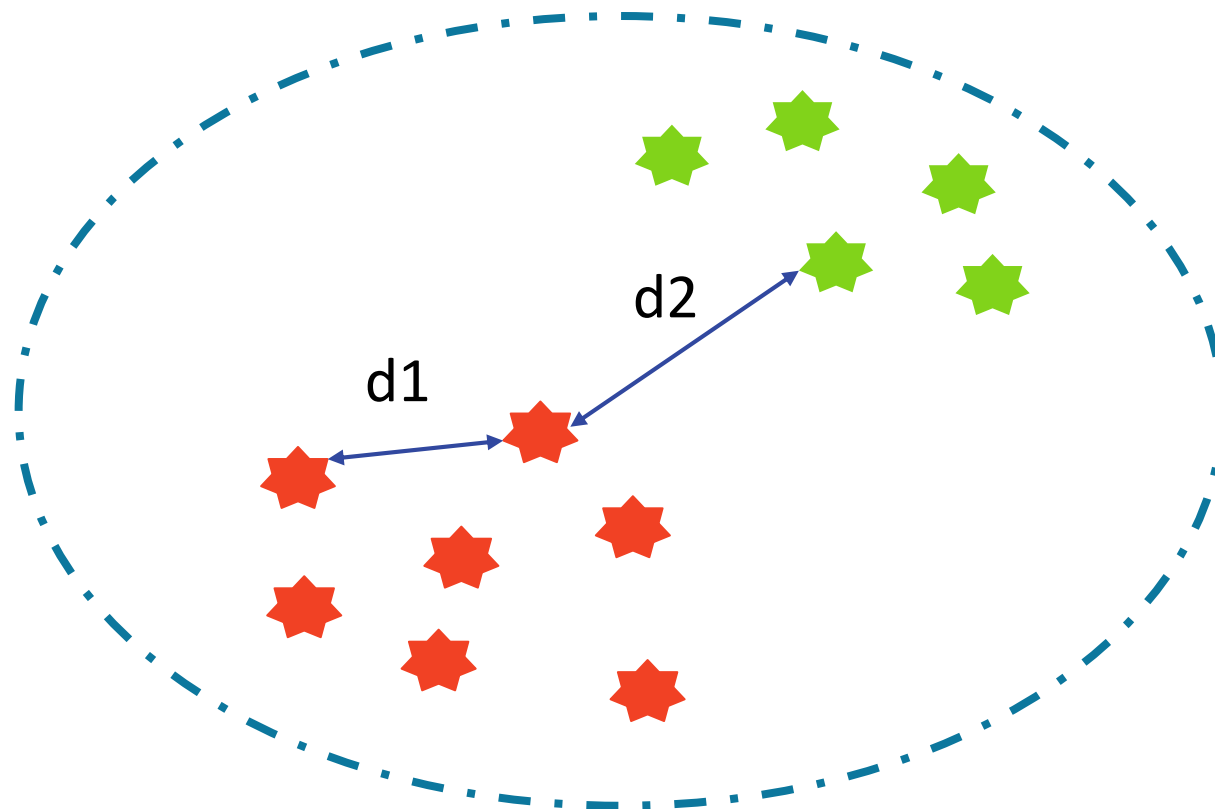
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Cosine similarity: 
$$S(f(x_i), f(x_j)) = \frac{f(x_i)^T f(x_j)}{\|f(x_i)\| \|f(x_j)\|}. \quad (1)$$



$$\mathcal{M} = \{(v_0, y_0), (v_1, y_1), \dots, (v_M, y_M)\}$$



First in first out  
***Memory bank:***

Feature1, label: 3
Feature2, label: 1
Feature3, label: 2
Feature4, label: 3
Feature5, label: 2
Feature6, label: 2
Feature7, label: 4

Capacity: M



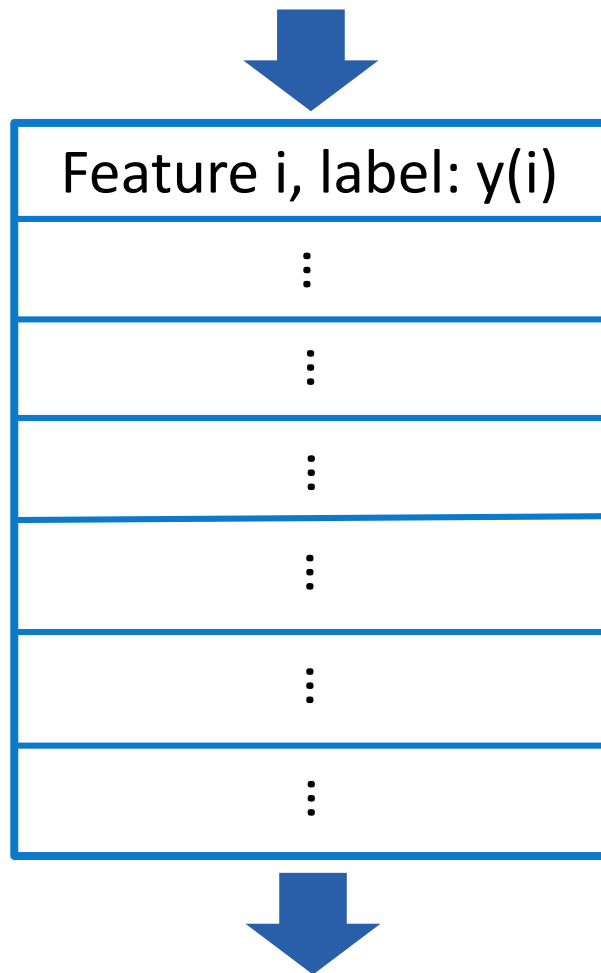
$$P_{\text{clean}}(i) = \frac{\exp(T(x_i, y_i))}{\sum_{k \in C} \exp(T(x_i, k))} \quad (2)$$

$$T(x_i, k) = \frac{1}{M_k} \sum_{(v_j, y_j) \in \mathcal{M}, y_j = k} S(f(x_i), v_j) \quad (3)$$

$M_k$  : The number of samples in class k in the memory bank

$T(x_i, k)$  : The **average similarity** between  $x_i$  and all the stored features  $v_j$  in class k

$P_{\text{clean}}(i) > m$ : clean sample



$$m = \frac{1}{\tau} \sum_{j=t-\tau}^t Q_j$$

$$\begin{aligned} \sum_{\substack{(v_j, y_j) \in \mathcal{M} \\ y_j = k}} \frac{S(f(x_i), v_j)}{M_k} &= \left( \frac{1}{M_k} \sum_{\substack{(v_j, y_j) \in \mathcal{M} \\ y_j = k}} \frac{v_j}{\|v_j\|} \right) \frac{f(x_i)}{\|f(x_i)\|} \\ &= w_k \frac{f(x_i)}{\|f(x_i)\|}, \end{aligned} \quad (5)$$

$$w_k = \frac{1}{M_k} \sum_{(v_j, y_j) \in \mathcal{M}, y_j = k} \frac{v_j}{\|v_j\|}. \quad (6)$$

Plugging Eq. (5) into Eq. (2),  $P_{\text{clean}}(i)$  can be expressed as:

$$P_{\text{clean}}(i) = \exp \left( w_{y_i} \frac{f(x_i)}{\|f(x_i)\|} \right) / \sum_{k \in \mathcal{C}} \exp \left( w_k \frac{f(x_i)}{\|f(x_i)\|} \right). \quad (7)$$

**Algorithm 1:** A training iteration of PRISM

**Input** :  $\mathcal{B} = \{(x_0, y_0), (x_1, y_1), \dots, (x_B, y_B)\}$ :  
 a given minibatch of data with size  $B$ ;  
 $f(\cdot)$ : a given deep metric model;

**Parameter:**  $\{w_k | k \in C\}$ : the set of mean feature  
 vectors of all classes, all initialized to  
 zero before training commences;

- 1 **for each**  $(x_i, y_i) \in \mathcal{B}$  **do**
- 2 | **if**  $w_{y_i} = \vec{0}$  **then**
- 3 | |  $P_{\text{clean}}(i) = 1$ ;
- 4 | **else**
- 5 | | Calculate  $P_{\text{clean}}(i)$  according to Eq. (7);
- 6 | **end**
- 7 **end**
- 8 Calculate the threshold  $m$  using TRM or sTRM;
- 9 Initialize  $\mathcal{B}_{\text{clean}}$  as an empty set;
- 10 **for each**  $(x_i, y_i) \in \mathcal{B}$  **do**
- 11 | **if**  $P_{\text{clean}}(i) > m$  **then**
- 12 | | Add  $(f(x_i), y_i)$  to  $\mathcal{B}_{\text{clean}}$ ;
- 13 | **end**
- 14 **end**
- 15 Enqueue  $\mathcal{B}_{\text{clean}}$  into the Memory Bank
- 16 **for each**  $(v_i, y_i) \in \mathcal{B}_{\text{clean}}$  **do**
- 17 | Update  $w_{y_i}$  according to Eq. (6);
- 18 **end**
- 19 Calculate loss  $L(\mathcal{B}_{\text{clean}})$  and update the parameters  
 of  $f(\cdot)$

More formally, the loss for mini-batch  $\mathcal{B}$  is

$$\begin{aligned} L_{\text{batch}}(\mathcal{B}) &= \sum_{\substack{(x_i, y_i) \in \mathcal{B}, (x_j, y_j) \in \mathcal{B} \\ y_i \neq y_j}} \max(S(f(x_i), f(x_j)) - \lambda, 0) \\ &\quad - \sum_{\substack{(x_i, y_i) \in \mathcal{B}, (x_j, y_j) \in \mathcal{B} \\ y_i = y_j}} S(f(x_i), f(x_j)) \end{aligned} \quad (8)$$

**Total Loss = (8)+(9)**

$$\begin{aligned} L_{\text{bank}}(\mathcal{M}, \mathcal{B}) &= \sum_{\substack{(x_i, y_i) \in \mathcal{B}, (v_j, y_j) \in \mathcal{M} \\ y_i \neq y_j}} \max(S(f(x_i), v_j) - \lambda, 0) \\ &\quad - \sum_{\substack{(x_i, y_i) \in \mathcal{B}, (v_j, y_j) \in \mathcal{M} \\ y_i = y_j}} S(f(x_i), v_j). \end{aligned} \quad (9)$$

Table 1: Precision@1 (%) on CARS, SOP, and CUB dataset with symmetric label noise.

Noisy Label Rate	CARS			SOP			CUB		
	10%	20%	50%	10%	20%	50%	10%	20%	50%
<i>Algorithms for image classification under label noise</i>									
Co-teaching [11]	73.47	70.39	59.55	62.60	60.26	52.18	53.74	51.12	45.01
Co-teaching+ [52]	71.49	69.62	62.35	63.44	67.93	58.29	53.31	51.04	45.16
Co-teaching [11] w/ Temperature [53]	77.51	76.30	66.87	73.71	71.97	64.07	55.25	54.18	50.65
F-correction [31]	71.00	69.47	59.54	51.18	46.34	48.92	53.41	52.60	48.84
<i>DML with Proxy-based Losses</i>									
FastAP [6]	66.74	66.39	58.87	69.20	67.94	65.83	54.10	53.70	51.18
nSoftmax [53]	72.72	70.10	54.80	70.10	68.90	57.32	51.99	49.66	42.81
ProxyNCA [26]	69.79	70.31	61.75	71.10	69.50	61.49	47.13	46.64	41.63
Soft Triple [32]	76.18	71.82	52.53	68.60	55.21	38.45	51.94	49.14	41.46
<i>DML with Pair-based Losses</i>									
MS [43]	66.31	67.14	38.24	69.90	67.60	59.58	57.44	54.52	40.70
Circle [37]	71.00	56.24	15.24	72.80	70.50	41.17	47.48	45.32	12.98
Contrastive Loss [7]	72.34	70.93	22.91	68.70	68.80	61.16	51.77	51.50	38.59
Memory Contrastive Loss (MCL) [46]	74.22	69.17	46.88	79.00	76.60	67.21	56.72	50.74	31.18
<b>MCL + PRISM (Ours)</b>	<b>80.06</b>	<b>78.03</b>	<b>72.93</b>	<b>80.11</b>	<b>79.47</b>	<b>72.85</b>	<b>58.78</b>	<b>58.73</b>	<b>56.03</b>

Table 2: Precision@1 (%) on CARS, SOP, and CUB with Small Cluster label noise.

Noisy Label Rate	CARS		SOP		CUB	
	25%	50%	25%	50%	25%	50%
<i>Algorithms for image classification under label noise</i>						
Co-teaching	70.57	62.91	61.97	58.08	51.75	48.85
Co-teaching+	70.05	61.58	62.57	59.27	51.55	47.62
Co-teaching w/ Temperature	75.26	66.19	70.19	68.50	54.59	48.32
<i>DML with Proxy-based Losses</i>						
FastAP	62.49	53.07	70.66	67.55	52.18	48.46
nSoftmax	71.61	62.29	70.00	61.92	49.61	41.78
ProxyNCA	69.50	58.34	67.95	62.25	42.07	36.48
Soft Triple	73.26	66.66	<b>73.63</b>	64.14	56.18	50.35
Soft Triple + PRISM (Ours)	<b>77.60</b>	<b>70.45</b>	70.99	<b>69.38</b>	<b>57.61</b>	<b>54.27</b>
<i>DML with Pair-based Losses</i>						
MS	63.92	43.73	67.32	62.17	53.60	41.66
Circle	53.03	19.95	70.33	40.48	44.07	22.96
Contrastive Loss	65.60	26.45	68.25	64.27	47.27	39.43
Memory Contrastive Loss (MCL)	69.46	36.43	75.61	68.71	52.25	41.58
MCL + PRISM (Ours)	<b>77.08</b>	<b>68.26</b>	<b>78.56</b>	<b>73.84</b>	<b>55.77</b>	<b>53.46</b>

Table 3: Precision@1 (%) and Mean Average Precision@R (%) on CARS-98N and Food-101N [21].

	CARS-98N		Food-101N	
	P@1	MAP@R	P@1	MAP@R
<i>Algorithms for image classification under label noise</i>				
Co-teaching	58.74	9.10	59.08	14.66
Co-teaching+	56.66	8.40	57.59	14.72
Co-teaching w/ Temperature	60.72	9.61	63.18	17.38
<i>DML with Proxy-based Losses</i>				
ProxyNCA	53.55	8.75	48.41	9.30
Soft Triple	63.36	10.88	63.61	16.23
Soft Triple + PRISM (Ours)	<b>64.81</b>	<b>11.21</b>	<b>64.46</b>	<b>17.53</b>
<i>DML with Pair-based Losses</i>				
MS	49.00	5.92	52.53	9.82
Contrastive	44.91	4.76	50.04	9.42
Memory Contrastive Loss (MCL)	38.73	3.34	<b>52.58</b>	<b>9.88</b>
MCL + PRISM (Ours)	<b>57.95</b>	<b>8.04</b>	52.47	9.64

Algorithm	Training Time (Seconds)
Memory Contrastive Loss (MCL)	1,679.22
MCL + PRISM without centers	12,294.76
MCL + PRISM with centers	1,777.38
Soft Triple	1,685.47
Soft Triple + PRISM with centers	1,767.97

**THANKS**